Effect of photogenerated carriers on the spectral diffusion of a quantum dot coupled to a photonic crystal cavity

Arka Majumdar,* Erik D. Kim, and Jelena Vučković

E.L. Ginzton Laboratory, Stanford University, Stanford, California 94305, USA (Received 23 July 2011; revised manuscript received 15 October 2011; published 4 November 2011)

We experimentally observe the effect of photogenerated carriers on the spectral diffusion of a quantum dot (QD) coupled to a photonic crystal (PC) cavity. In this system, spectral diffusion arises in part from charge fluctuations on the etched surfaces of the PC. We find that these fluctuations may be suppressed by photogenerated carriers, leading to a reduction of the measured QD linewidth by a factor of \sim 2 compared to the case where the photogenerated carriers are not present. This result demonstrates a possible means of countering the effects of spectral diffusion in QD-PC cavity systems and thus may be useful for quantum information applications where narrow QD linewidths are desired.

DOI: 10.1103/PhysRevB.84.195304

PACS number(s): 42.50.-p, 85.35.Be

I. INTRODUCTION

A single self-assembled quantum dot (QD) coupled to a high-quality (Q) factor semiconductor optical cavity has emerged in recent years as a promising system for developing on-chip quantum technologies.^{1–3} Although this solid-state cavity quantum electrodynamic (CQED) system behaves similarly to its atomic counterpart in a number of ways, the unavoidable interaction of the QD with its solid-state environment gives rise to phenomena specific to the solid-state system. For instance, the presence of acoustic phonons even at cryogenic temperatures has led to the observation of far off-resonant coupling between a QD and a cavity, where resonant optical excitation results in the emission of a photon at the cavity (QD) wavelength when the QD (cavity) is driven.^{4–6} In this case, phonon-mediated off-resonant coupling may provide a useful means of performing quantum state readout.⁷

Another important phenomenon arising from the solid-state nature of the QD-cavity system is the random trapping and untrapping of charges in the vicinity of the QD due to defects, leading to spectral diffusion of the QD optical transition energy.^{8–11} Spectral diffusion (or jitter) is generally considered detrimental to the optical properties of QDs as it leads to the broadening of optical emission lines.^{12–14} Studies of spectral diffusion in bulk self-assembled QD systems have attributed its observation to defects provided by the highly disordered QD wetting layer.^{9,15} Additionally, it has been postulated that the proximity of etched surfaces near the QD can lead to spectral diffusion due to defects provided by the etched surface roughness.¹⁶ Recent experimental studies of the linewidth of a QD off-resonantly coupled to a photonic crystal (PC) cavity mode have also observed broadening of QD linewidths that cannot simply be attributed to a pure dephasing process.¹⁷ This is not surprising considering that in QD-PC cavity systems both the wetting layer and the presence of etched surfaces are expected to contribute to spectral diffusion, particularly for ODs close to the holes of the photonic lattice. Further, each contribution is expected to manifest under different system conditions. For instance, wetting layer defects predominantly trap charges through the ionization of excitons generated in the vicinity of the QD by above-band (AB) optical excitation. This contribution to spectral diffusion has been shown to depend on the strength of the AB laser and is absent at very low

excitation powers.⁹ For trap states provided by the rough etched surfaces of the photonic crystal, fluctuating surface charges are anticipated to contribute to spectral diffusion even in the absence of AB optical excitation. It is unclear, however, how this contribution to spectral diffusion may be affected by above-band excitation, if it can be affected at all.

Here, we experimentally analyze the dependence of spectral diffusion on the power of an AB laser for a QD off-resonantly coupled to a PC cavity. Specifically, we perform QD linewidth measurements by scanning a narrow-bandwidth continuouswave (CW) laser across the QD resonance and observing optical emission from the detuned cavity. In the absence of AB pumping, we observe a broadened QD linewidth and attribute this broadening to fluctuating surface charges on the nearby etched surfaces. Surprisingly, we find that this contribution to spectral diffusion is suppressed in the presence of AB excitation. We attribute this suppression to the filling of trap states in nearby etched surfaces by photogenerated carriers leading to a drastic reduction of charge fluctuations. This in turn dramatically reduces the experimentally observed QD linewidth. For low AB laser powers, spectral diffusion becomes negligible and the QD linewidth exhibits the standard power broadening as the CW laser power is increased. These results demonstrate an optical excitation regime in which spectral diffusion may be overcome and provide a simple means of countering the degradation of the optical properties of QDs in PC structures. This approach could thus prove useful in QD-PC cavity based quantum technologies that benefit from narrower emitter linewidths.

II. QUANTUM DOT LINEWIDTH BROADENING

The effect of the spectral diffusion is reflected in the measurement of the QD linewidth. In the linear response regime, the QD lineshape is characterized by the QD susceptibility¹⁸

$$\chi(t) \propto \mathcal{F}\left[e^{(i\omega_0 - \frac{\gamma(\omega_0)}{2})t} \left\langle e^{-i\int_0^t d\tau \delta\omega(\tau)} \right\rangle\right] \tag{1}$$

where \mathcal{F} denotes the Fourier transform, ω_0 is the QD resonance frequency, $\gamma(\omega_0)$ is the radiative QD linewidth, and the statistical average is taken over all the possible frequencies at different times τ . The effect of spectral diffusion is reflected in this statistical average. This average depends on the underlying probability distribution of the random environment. Assuming a Gaussian fluctuation, by Cumulant expansion (and noting the odd moments are zero), we can write

$$\left\langle e^{-i\int_0^t d\tau \,\delta\omega(\tau)} \right\rangle = e^{-\frac{1}{2}\int_0^t d\tau_1 \int_0^t d\tau_2 \langle \delta\omega(\tau_1)\delta\omega(\tau_2) \rangle}.$$
 (2)

Assuming an exponential correlation function (with variance Γ and correlation time τ_c) of the form

$$\langle \delta \omega(\tau_1) \delta \omega \tau_2 \rangle = \Gamma^2 e^{-\frac{|\tau_1 - \tau_2|}{\tau_c}} \tag{3}$$

we find that

$$\left\langle e^{-i\int_{0}^{t}d\tau\delta\omega(\tau)}\right\rangle = e^{-\Phi(t)} \tag{4}$$

with

$$\Phi(t) = \Gamma^2 \tau_c^2 [e^{-t/\tau_c} + t/\tau_c - 1].$$
(5)

Hence, we can model the effect of the fluctuating environment by two quantities: the standard deviation Γ and the correlation time τ_c . In the limit of long measurement time ($t \gg \tau_c$), the linewidth of the QD is given by $(\gamma + \Gamma^2 \tau_c)$, where γ comes from the Lorentzian line shape of the QD and $\Gamma^2 \tau_c$ is the contribution of the fluctuating environment. In this article, we perform two separate sets of experiments to determine these characteristic quantities of the fluctuating environment. From the first set of experiments, we obtain a measure of the lifetime of the charges in the traps and estimate the correlation time τ_c to be approximately 22 ns. In the second set of experiments, we show how photogenerated carriers can mitigate the effect of the spectral diffusion that is present in the absence of any aboveband excitation. From experimental results (see Sec. IV) we determine the broadening due to the fluctuating environment and estimate the quantity $\Gamma^2 \tau_c$ to be approximately 8.7 GHz, corresponding to $\Gamma \sim 600$ MHz. We note that as these values were obtained for two different QDs on the same wafer, they provide only order-of-magnitude estimates.

III. QUANTUM DOT CHARGING AND MODULATION

All the experiments are performed in a helium-flow cryostat at cryogenic temperatures (~30-55 K) on self-assembled InAs QDs embedded in a GaAs photonic crystal cavity.^{2,4} The 160-nm GaAs membrane used to fabricate the photonic crystal is grown by molecular beam epitaxy on top of a GaAs (100) wafer. The GaAs membrane sits on a 918-nm thick sacrificial layer of Al_{0.8}Ga_{0.2}As. Under the sacrificial layer, a 10-period distributed Bragg reflector, consisting of a quarterwave AlAs/GaAs stack, is used to increase the collection into the objective lens.² The photonic crystal was fabricated using electron beam lithography, dry plasma etching, and wet etching of the sacrificial layer in hydrofluoric acid (6%). The inset of Fig. 1 shows the scanning electron micrograph of a fabricated photonic crystal cavity. A cross-polarized confocal microscopy setup is used to probe the QDs, both in photoluminescence (PL) as well as under resonant excitation as shown in Fig. $1.^{2,4}$

In the first set of experiments, we investigate the time scale on which carriers generated by the above-band (AB) laser affect the QD environment. These experiments are used to provide a measure of correlation time τ_c associated with the fluctuating surface charges. To perform these measurements, we first identify a strongly coupled QD-cavity system in PL



FIG. 1. (Color online) The cross-polarized confocal microscopy setup used to probe the coupled QD-cavity system. The inset shows a scanning electron micrograph of the fabricated PC cavity. OL and PBS stand for objective lens and polarizing beam splitter, respectively.

studies by observing the anticrossing of the QD and cavity resonances that occurs as the temperature is varied. We then probe the system by measuring the transmission of a resonant continuous wave laser through the cavity. In the absence of the AB laser excitation, we observe a Lorentzian line shape for the cavity transmission, indicating that there is no QD coupled to the cavity despite the fact that coupling is observed in PL studies. When the weak AB laser is turned on, however, we observe a drastic change in the transmission spectrum as shown in Fig. 2(a). The spectrum now appears to show two QDs strongly coupled to the cavity as indicated by the presence of two dips in the transmission spectrum. Inset of Fig. 2(a) shows the theoretically predicted spectrum of cavity transmission, in the absence and presence of two coupled QDs. The experimentally obtained spectra qualitatively match well with the numerical calculation. We note that, in presence of two strongly coupled QDs, the total loss of the system is distributed among the three peaks and an apparent narrowing of the bare cavity linewidth is observed. Similar simultaneous strong coupling of two QDs with a semiconductor microcavity has previously been observed by other groups.^{19–21} This dramatic change in the transmission spectrum could be caused by the capturing of optically generated carriers by the QD, which leads to the formation of charged excitons and a discrete shift in the QD resonance wavelength, which in this case aligns it with the cavity.²² Another possibility is that both ODs are in the optically dark state, but are brought back to the optically active states (aligned with the cavity resonance) by the action of the AB laser. However, in the previous experiments on QD blinking it has been shown that QDs remain in such optically dark states typically for approximately several hundred nanoseconds,²³ which is much smaller than our experimental integration time. Therefore, this would mean that splitting in the transmission spectrum in Fig. 2(a) should be observed even without the AB laser (although with smaller contrast). Another possible explanation is that the linewidth broadening caused by spectral diffusion suppresses the dips in the transmission spectrum. In the presence of the AB laser, the spectral diffusion is reduced (as will be discussed later in the paper), leading to a reduction of QD linewidths and the appearance of the dips in the transmission spectrum. We note that in presence of the AB laser, the amount of light coming



FIG. 2. (Color online) (a) Effect of the above-band (AB) laser on the transmission spectrum of a strongly coupled QD-cavity system. The arrow shows the wavelength of the other (resonant) CW laser, whose transmission is modulated by the AB laser in (b) and (c). Inset shows numerically simulated plots of a cavity with and without two strongly coupled QDs. The theoretical results qualitatively match the experimental data well. (b) The transmitted laser power in steady state when the AB laser is turned on and off manually, at intervals of several 10s. This shows the DC characteristics of the modulation. (c) The temporal dynamics of the QD-cavity system: the transmitted laser output as a function of time (black plot). The shown modulation signal (red) is used to modulate the above-band laser. From exponential fits (green) we estimate a time constant of \sim 22 ns, which is obtained as the inverse of the total diffusion rate [equal to the sum of the rates for the rising edge (i.e., carrier capture) and the falling edge (i.e., carrier release)]. (d) The on-off ratio of the transmitted laser as a function of the modulation frequency.

out of the cavity due to PL is negligible compared to the light transmitted through the cavity.

Next, we study the time dynamics of this resonance shift to obtain a measure of the time scale on which the charge environment surrounding the OD fluctuates. This is done by measuring the transient response of the transmitted resonant laser power to modulation of the AB laser. We note that this type of modulation is different from the all-optical modulation reported in Ref. 24, where the OD shifts continuously with increasing AB laser power and the modulation is caused by the screening of the built-in electric field by photogenerated carriers (in the present case, we use an undoped wafer, while Ref. 24 employed a wafer with a pin junction where such effect was significant). To obtain optimal modulation contrast we tune the CW laser to the dip in the cavity transmission spectrum [shown by the arrow in Fig. 2(a)]. Figure 2(b) shows the DC modulation behavior when the above-band laser is manually turned on and off at varying time intervals and the resonant laser transmission is measured at steady state. To measure temporal dynamics, we apply a square-wave modulation to the above-band laser and measure the CW laser transmission [at the wavelength indicated by an arrow in Fig. 2(a)] by a single photon counter and a picosecond time analyzer triggered by the modulated above-band laser.²⁰ We note that

for this experiment, the powers of the above-band laser and the resonant CW laser are, respectively, 15 nW and 250 nW as measured in front of the objective lens of the confocal microscopy setup. Figure 2(c) shows the modulated cavity transmission output with time, for a modulation frequency of 2 MHz. We observe an exponential rise (decay) of the resonant laser transmission when the AB laser is turned on (off). These two time scales provide estimates of how much time it takes for the charges to get trapped or untrapped in the vicinity of the QD. We fit the exponentials and obtain a rising time constant of $\tau_r \sim 30$ ns and a decay time constant of $\tau_d \sim 80$ ns. From these two measurements we estimate the time scale of the fluctuation of charges to be $\tau_c = \frac{\tau_r \tau_d}{\tau_r + \tau_d} \sim 22$ ns. This shows that the maximum modulation speed is $1/(2\pi\tau_c) \sim 7$ MHz. Finally, Fig. 2(d) shows the on-off ratio of the transmitted CW laser as a function of the modulation frequency of the above-band laser demonstrating that the maximum modulation speed is approximately on the order of \sim 7 MHz. We note that this measurement of correlation time only provides an order-of-magnitude estimation.

IV. QUANTUM DOT LINEWIDTH BROADENING

Having obtained a measure of the correlation time associated with local charge fluctuations, we now turn to experimental measurements of the broadening of QD linewidths by spectral diffusion. For this set of experiments, we consider a system where a QD is far off-resonantly coupled to a PC cavity mode. For this particular system the dot is 1.4 nm bluedetuned from the cavity (the dot and cavity are, respectively, at 934.9 and 936.3 nm) [see Fig. 3(a)]. QD linewidths are obtained by measuring the off-resonant cavity emission as the CW laser is scanned through the QD resonance, similar to experiments reported in Ref. 17. We observe saturation of the cavity emission and power broadening of the QD with increasing excitation laser power. We emphasize that in the experimental data shown in Fig. 3, the additional AB laser is not used, and the QD is driven only by the resonant laser. By simultaneously fitting the cavity emission with the model $I_{\text{sat}}\tilde{P}/(1+\tilde{P})$ [Fig. 3(b)] and the QD linewidth with the model $\Delta \omega_0 \sqrt{1 + \tilde{P}}$ [Fig. 3(c)],²⁵ we find that the observed QD linewidth is significantly smaller than what is expected from ordinary power broadening of a two level system [the dashed line in Fig. 3(c)]. Here, I_{sat} is the saturated cavity emission intensity, $\Delta \omega_0$ is the QD linewidth at the limit of zero excitation power and \tilde{P} is proportional to the laser intensity at the position of the QD. Simple theoretical analysis shows that the QD linewidth exhibits power broadening similar to that of a two-level system,²⁶ thus showing that the cavity readout does not affect the QD linewidth significantly. This unusual broadening behavior cannot be explained by an increasing pure dephasing rate with increasing laser power or excitation induced dephasing,²⁷ since those effects would lead to a broader linewidth than that predicted by standard power broadening. In fact, the nature of the broadening indicates a power-independent broadening mechanism.

We thus consider spectral diffusion as a means of modeling this additional power-independent broadening. We note that spectral diffusion is indeed power independent when the laser



FIG. 3. (Color online) QD spectroscopy by off-resonant dotcavity coupling: (a) The spectrum showing the laser resonantly driving the QD and the emission from an off-resonant cavity. A logarithmic scale is used to show both the strong laser and the weak cavity emission. (b) Cavity emission as a function of the power of the laser that is driving the QD resonantly. (c) QD linewidth $\Delta \omega$ measured by monitoring the cavity emission by scanning the laser across the QD. $\Delta \omega$ is plotted as a function of the excitation laser power. We find that the standard power-broadening model overestimates the measured QD linewidth (the dashed line). However, the model provides better agreement with experimental results when spectral diffusion is taken into account (solid line).

is resonant with the QD. The effect of spectral diffusion is modeled as a Voigt line shape, which is a convolution of a Lorentzian line shape (the actual QD linewidth $\Delta \omega_L$) and a Gaussian line shape (the spectral fluctuations with a linewidth of $\Delta \omega_D$). The full width half maximum $\Delta \omega_V$ of a Voigt line shape is given by²⁸

$$\Delta\omega_V \approx A\Delta\omega_L + \sqrt{(1-A)^2}\Delta\omega_L^2 + \Delta\omega_D^2 \tag{6}$$

where the parameter A = 0.5346 is empirically determined. We use this model to fit the power-broadened line width, where $\Delta \omega_L = \Delta \omega_0 \sqrt{1 + \tilde{P}}$. The model fits the experimental data very well, with parameters $\Delta \omega_0/2\pi = 4.7$ GHz and $\Delta \omega_D/2\pi = 8.7$ GHz. These results support the theory that spectral diffusion is caused by the trap states present on the etched surfaces of the photonic crystal. These traps can be randomly charged and discharged, resulting in a fluctuating charge environment that can modify the QD resonance frequency by random DC Stark shifts. As we perform timeaveraged measurements on time scales much longer than the correlation time estimated in the preceding set of experiments, the measured QD linewidth is a statistical mixture of the QD resonances at different resonance frequencies.

We now repeat these experiments in the presence of an above-band laser. Although the QD transition energy is not shifted in the presence of the PL laser, we observe a significant reduction in the measured QD linewidth (by a factor of \sim 2) and



FIG. 4. (Color online) Effect of the AB laser on the QD spectrum as measured though off-resonant cavity emission. In the absence of the AB laser, we observe a broad QD linewidth. However, in the presence of this laser, a significant linewidth narrowing is observed. The increased background with the AB laser on is caused by the PL generated by the AB laser. The inset shows the QD linewidth measured as a function of the AB laser power.

an increase in the off-resonant cavity emission (Fig. 4). The resonant laser power is kept at the same value ($\sim 100 \text{ nW}$) as used in the measurements of Fig. 3. The increased background in the cavity emission in the presence of the AB laser is caused by the small amount of PL generated by this laser. We find that the QD exhibits a Lorentzian line shape in presence of the AB laser, but shows a nearly Gaussian line shape in the absence of the AB laser. We attribute this difference to the fact that one of the effects of the AB laser is to create carriers that subsequently fill all the empty traps near the QD, thereby reducing spectral fluctuations. The dependence of the QD linewidth as a function of AB laser power is shown in the inset of Fig. 4. With increasing AB laser power, the PL adds noise to the off-resonant cavity emission, making linewidth measurements difficult. However, we do observe a slight increase in the QD linewidth with increasing AB laser power, consistent with previous studies.⁹ We note that an AB laser can cause multiple effects such as an abrupt change in the QD resonance frequency,²² or saturation of the QD. Hence this type of linewidth narrowing in the presence of the AB laser is not observed for all the QDs. However, the additional power-independent broadening is present in the absence of AB pumping for all QDs studied.

For this particular QD, we also perform a power-dependent study of the QD linewidth and cavity emission in the presence of the AB laser. The AB laser power is kept constant throughout experiments. The data in the absence of the AB laser is the same as shown in Fig. 3. Figure 5(a) shows the off-resonant cavity emission intensity as a function of the excitation laser power both in the presence and absence of the AB laser. In the presence of the AB laser, we observe an increased cavity emission and also a saturation trend at lower laser power (shown by the fit). However, with increasing excitation laser power, the cavity emission decreases. This decrease in the cavity emission may be due to the presence of other QD excitonic states. The fact that those states are present only with the AB excitation may be an indication that these other



FIG. 5. (Color online) (a) Off-resonant cavity emission as a function of the laser power driving the QD resonantly for two cases: with and without the additional, weak above-band laser. (b) Extracted QD linewidth as a function of the resonant driving laser power. A much narrower linewidth is observed in the presence of the AB laser at lower excitation powers. Also, the QD linewidth follows a simple power broadening with the excitation laser power when the AB laser is present. In the absence of the AB laser, we observe an additional power-independent broadening, which can be explained by spectral diffusion of the QD.

excitonic states are multiply charged states arising from the capture of multiple photogenerated carriers.²⁹ Figure 5(b) shows the measured QD linewidth as a function of the excitation laser power both in the presence and absence of the AB laser. We find that the QD linewidth is narrower with AB laser on at lower laser excitation power. In fact, the QD linewidth in that case follows ordinary power broadening (as

shown by the solid line fit), with $\Delta \omega_0/2\pi = 4.7$ GHz, the same as the Lorentzian linewidth obtained from the fit to the linewidth data with spectral diffusion.

V. CONCLUSION

In summary, we have presented experimental studies showing the effect of the photogenerated carriers on spectral diffusion in the QD-PC cavity QED system. We first showed that the transmission spectrum of the strongly coupled QD-PC cavity system can be modified with a very low power of the additional above-band laser. We also show the significant effect of spectral diffusion in resonant OD spectroscopy, when the QD is embedded in a photonic crystal cavity. This spectral diffusion can be mitigated by photogenerated carriers that serve to fill the trap states occurring at the etched surfaces of the PC. This significant reduction of the OD linewidth by the additional weak, above-band excitation is an attractive prospect for potential quantum information applications employing QDs in PC structures. For those applications benefiting from narrow QD linewidths, the results presented here demonstrate a relatively simple means of improving the optical quality of QDs and thus system performance.

ACKNOWLEDGMENTS

The authors acknowledge support provided by the NSF, Army Research Office (ARO), and ONR. E.K. acknowledges support from the Intelligence Community Postdoctoral Research Fellowship program. The authors acknowledge Dr. Pierre Petroff and Dr. Hyochul Kim for providing the QD sample.

*arkam@stanford.edu

- ¹A. Faraon, A. Majumdar, D. Englund, E. Kim, M. Bajcsy, and J. Vučković, New J. Phys. **13**, 055025 (2011).
- ²D. Englund, A. Faraon, I. Fushman, N. Stoltz, P. Petroff, and J. Vučković, Nature (London) **450**, 857 (2007).
- ³A. Imamoglu, D. D. Awschalom, G. Burkard, D. P. DiVincenzo, D. Loss, M. Sherwin, and A. Small, Phys. Rev. Lett. **83**, 4204 (1999).
- ⁴D. Englund, A. Majumdar, A. Faraon, M. Toishi, N. Stoltz, P. Petroff, and J. Vučković, Phys. Rev. Lett. **104**, 073904 (2010).
- ⁵S. Ates, S. M. Ulrich, A. Ulhaq, S. Reitzenstein, A. Lffler, S. Hfling, A. Forchel, and P. Michler, Nature Photon. **3**, 724 (2009).
- ⁶C. Roy and S. Hughes, Phys. Rev. Lett. 106, 247403 (2011).
- ⁷A. Majumdar, A. Papageorge, E. D. Kim, M. Bajcsy, H. Kim, P. Petroff, and J. Vučković, Phys. Rev. B **84**, 085310 (2011).
- ⁸A. Berthelot, I. Favero, G. Cassabois, C. Voisin, C. Delalande, P. Roussignol, R. Ferreira, and J. M. Gérard, Nature Phys. **2**, 759 (2006).
- ⁹H. D. Robinson and B. B. Goldberg, Phys. Rev. B 61, R5086 (2000).
- ¹⁰J. Seufert, R. Weigand, G. Bacher, T. Kummell, A. Forchel, K. Leonardi, and D. Hommel, Appl. Phys. Lett. **76**, 1872 (2000).
- ¹¹V. Türck, S. Rodt, O. Stier, R. Heitz, R. Engelhardt, U. W. Pohl, D. Bimberg, and R. Steingrüber, Phys. Rev. B 61, 9944 (2000).

- ¹²H. Kamada and T. Kutsuwa, Phys. Rev. B 78, 155324 (2008).
- ¹³G. Sallen, A. Tribu, T. Aichele, R. André, L. Besombes, C. Bougerol, M. Richard, S. Tatarenko, K. Kheng, and J.-P. Poizat, Phys. Rev. B 84, 041405 (2011).
- ¹⁴G. Sallen, A. Tribu, T. Aichele, R. André, L. Besombes, C. Bougerol, M. Richard, S. Tatarenko, K. Kheng, and J.-P. Poizat, Nature Photon. 4, 696 (2010).
- ¹⁵R. Heitz, T. R. Ramachandran, A. Kalburge, Q. Xie, I. Mukhametzhanov, P. Chen, and A. Madhukar, Phys. Rev. Lett. **78**, 4071 (1997).
- ¹⁶C. F. Wang, A. Badolato, I. Wilson-Rae, P. M. Petroff, E. Hu, J. Urayama, and A. Imamoglu, Appl. Phys. Lett. 85, 3423 (2004).
- ¹⁷A. Majumdar, A. Faraon, E. D. Kim, D. Englund, H. Kim, P. Petroff, and J. Vučković, Phys. Rev. B 82, 045306 (2010).
- ¹⁸R. Kubo, A Stochastic Theory of Line Shape (Wiley, New York, 2007), pp. 101–127.
- ¹⁹S. Reitzenstein *et al.*, Opt. Lett. **31**, 1738 (2006).
- ²⁰A. Faraon, A. Majumdar, H. Kim, P. Petroff, and J. Vučković, Phys. Rev. Lett. **104**, 047402 (2010).
- ²¹A. Laucht, J. M. Villas-Bôas, S. Stobbe, N. Hauke, F. Hofbauer, G. Böhm, P. Lodahl, M.-C. Amann, M. Kaniber, and J. J. Finley, Phys. Rev. B 82, 075305 (2010).

- ²²E. D. Kim, A. Majumdar, H. Kim, P. Petroff, and J. Vučković, Appl. Phys. Lett. **97**, 053111 (2010).
- ²³C. Santori, D. Fattal, J. Vučković, G. S. Solomon, E. Waks, and Y. Yamamoto, Phys. Rev. B **69**, 205324 (2004).
- ²⁴D. Englund, A. Faraon, A. Majumdar, N. Stoltz, P. Petroff, and J. Vučković, Opt. Express **17**, 18651 (2009).
- ²⁵E. B. Flagg, A. Muller, J. W. Robertson, S. Founta, D. G. Deppe, M. Xiao, W. Ma, G. J. Salamo, and C. K. Shih, Nature Phys. 5, 203 (2009).
- ²⁶A. Majumdar, E. D. Kim, Y. Gong, M. Bajcsy, and J. Vučković, Phys. Rev. B **84**, 085309 (2011).
- ²⁷A. J. Ramsay, A. V. Gopal, E. M. Gauger, A. Nazir, B. W. Lovett, A. M. Fox, and M. S. Skolnick, Phys. Rev. Lett. **104**, 017402 (2010).
- ²⁸J. Olivero and R. Longbothum, J. Quant. Spectrosc. Radiat. Transfer 17, 233 (1977).
- ²⁹R. J. Warburton, C. Schäflein, D. Haft, F. Bickel, A. Lorke, K. Karrai, J. M. Garcia, W. Schoenfeld, and P. M. Petroff, Nature (London) **405**, 916 (2000).